## BRONX COMMUNITY COLLEGE of the City University of New York

## DEPARTMENT OF MATHEMATICS & COMPUTER SCIENCE MTH6 Review Sheet III

## 1. Simplify:

(a)  $\sqrt{108}$ 

(b)  $\sqrt{180}$  (c)  $\sqrt[3]{40}$ 

2. Perform the indicated operations and simplify (all variables represent positive real numbers):

(a)  $5\sqrt{12} - 4\sqrt{3} + \sqrt{75}$  (b)  $(2\sqrt{3})(3\sqrt{5})$ 

(c)  $(4+\sqrt{2})(5-3\sqrt{2})$ 

(d)  $(8+2\sqrt{3})^2$ 

(e)  $(1-2\sqrt{11})(1+2\sqrt{11})$  (f)  $\sqrt{\frac{7}{18}}$ 

(g)  $\frac{\sqrt{2}}{\sqrt{5}}$ 

(h)  $\frac{\sqrt{3}}{\sqrt{x}}$ 

(i)  $\frac{\sqrt[3]{2x}}{\sqrt[3]{9x^2}}$ 

(j)  $\frac{1}{2+\sqrt{3}}$ 

(k)  $\frac{\sqrt{x} - \sqrt{y}}{\sqrt{x} + \sqrt{y}}$ 

3. Perform the indicated operations and simplify (all variables represent positive real numbers):

(a)  $64^{-2/3}$ 

(b)  $\left(\frac{9}{16}\right)^{-1/2}$ 

(c)  $(64x^3y \cdot xy^5)^{4/3}$ 

(d)  $\left(\frac{27x^5y}{8u^3}\right)^{1/3}$ 

(e)  $\left(\frac{8x^{\frac{1}{4}}y^{-\frac{3}{4}}}{x^{-\frac{1}{2}}y^3}\right)^{2/3}$ 

4. Solve the equation.

(a)  $\sqrt{2x+3}-3=0$ 

(b)  $\sqrt{2x+5} = 3\sqrt{x-1}$  (c)  $\sqrt{3x+4} - x = 2$ 

5. Perform the indicated operations of complex numbers and simplify:

(a)  $i^{173}$ 

(b) (2-3i)(5-7i)-(3-2i)

(c)  $\frac{4-7i}{5+3i}$ 

**6.**Solve the equation by completing the square.

(a) 
$$x^2 + 6x - 12 = 0$$
 (b)  $x^2 + 4x + 6 = 0$  (c)  $2x^2 - 8x = 0$ 

(b) 
$$x^2 + 4x + 6 = 0$$

(c) 
$$2x^2 - 8x = 0$$

7. Solve the equation by quadratic formula.

(a) 
$$x^2 - 2x - 6 = 0$$
 (b)  $x^2 - 3x = 0$  (c)  $x^2 = 8$ 

(b) 
$$x^2 - 3x = 0$$

(c) 
$$x^2 = 8$$

**8.** Solve the equation by any method.

(a) 
$$2x^2 + 18 = 0$$

(b) 
$$x^2 + 4x + 20 = 0$$
 (c)  $4x^2 + 5x - 6 = 0$ 

(c) 
$$4x^2 + 5x - 6 = 0$$

(d) 
$$(2x-3)(x+4) = 4$$
 (e)  $x^4 - 7x^2 + 12 = 0$ 

(e) 
$$x^4 - 7x^2 + 12 = 0$$

**9.** Determine the exact value of:

(a) 
$$\cos 60^{\circ}$$

(b) 
$$\csc 45^{\circ}$$

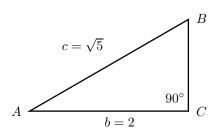
(b) 
$$\cos 45^{\circ}$$
 (c)  $\sin 30^{\circ} - \cos 45^{\circ}$ 

**10.** Use the triangle to find:

(a) 
$$\cos A$$

(b) 
$$\csc A$$

(c) 
$$\tan B$$



11. Given that  $\triangle ABC$  is a right triangle with  $C = 90^{\circ}$ , find the missing sides.

(a) 
$$\cos A = \frac{1}{3}, \ b = 2$$

(b) 
$$\tan A = \frac{2}{3}, \ b = 6$$

(c) 
$$\cos B = \frac{1}{4}, \ c = 12$$

- The angle of elevation of the top of a tree is 60° from an observation point 80 feet from the base of the tree. Find the height of the tree.
- 13. Bill is standing on top of a 175 foot cliff overlooking a lake. The measure of the angle of depression to a boat is  $30^{\circ}$ .
- (a) How far, exactly, is the boat from the foot of the cliff?
- (b) How far is the boat from Bill?
  - 01/2022 YH, IP