

## Topic #7: Formal Definitions (Math 31)

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1. Goals:
  - a. Formal Definition of Limit
  - b. Calculating Limits from the formal definition
2. Some pre-algebra:
  - a. Ex: Add and divide rational expressions
3. Informal Definition.
  - a. Recall definition of  $f'(x)$  = the slope of the tangent line at  $x$  of the function  $f$
  - b. Show animation from book web link page 215.
  - c. Draw  $f'$  from  $f$ : Discuss some values and + or – before graphing.
4. Formal Definition
  - a. Give visual way of finding tangent line as limit of secant lines.
  - b. DO: With string and volunteers and make table of  $h$  vs. slope values.
    - i. Need:
      1. Point Person
      2. 2 Line People
      3. An Eye
      4. Data Collector
    - ii. Do in groups on board; I draw
  - c. TWO definitions by limit (See picture page 216)
5. Calculate derivatives using formal definition
  - a. Examples [DO: First with numbers for  $x$ ; then just  $x$ ; find some eqns of tan lines]
    - i. For any line (use both definitions)
    - ii. Ex:  $x^2$  and with coefficients.
    - iii. Derivative of  $3/x$
    - iv.  $(x^3 - x)$