MTH 23.5 LECTURE NOTES (Ojakian) Topic 11: Probability - Contingency Tables and Trees

OUTLINE

References (Algebra Book: None; Statistics Book: 3.4, 3.5)

1. Contigency Tables

2. Trees

1. Contingency tables

- (a) Example 3.20 (page 183)
- (b) Students: Try It 3.20 (page 184)
- (c) Example 3.22 (page 186-187): With probabilities instead of quantities.

2. <u>Trees</u>

- (a) Example: Like 3.25 page 191 (BUT, do with replacement)
- (b) Example: Now do page 191 (without replacement). See schematic on page 192.
- (c) Students: Do example 3.26 (page 192-193).

3. Tree Examples

(a) Note: WITH and WITHOUT replacement. Represent the following using tree diagrams.

PROBLEM 1. Two cards are drawn from a regular deck of 52 cards, with replacement.

- i. What is the probability that the first card is an ace and the second is a king?
- ii. What is the probability the first card is NOT an ace and the second is a king?

PROBLEM 2. Two cards are drawn from a regular deck of 52 cards, without replacement.

- i. What is the probability that the first card is an ace and the second is a king?
- ii. What is the probability the first card is NOT an ace and the second is a king? (watch out!)

PROBLEM 3. A jar contains 2 red marbles, 5 blue marbles, and 5 yellow marbles.

- i. Suppose you take 2 marbles, without replacement. What is the probability that you take 1 blue and 1 yellow, in any order.
- *ii.* Suppose you take 2 marbles, with replacement. What is the probability that you take 1 blue and 1 yellow, in any order.
- *iii.* Suppose you take 3 marbles, without replacement. What is the probability that all are red?
- iv. Suppose you take 3 marbles, without replacement. What is the probability that at least one is not red?