

MTH 23.5 LECTURE NOTES (Ojakian)

Topic 5: Order of Operations, Radicals

OUTLINE

References (**Algebra Book**: p.35-39; **Statistics Book**: None)

1. Radicals
 2. Absolute Value
 3. Order of Operations
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1. Some background mathematics: Radicals

- (a) Recall square roots

PROBLEM 1. Calculate the following: $\sqrt{16}$, $\sqrt{100}$

PROBLEM 2. Which of the following “make sense”: $\sqrt{16}$, $\sqrt{-16}$, $\sqrt{0}$

- (b) Inverses

PROBLEM 3.

- Pick your favorite number: square it, then take its square root. What happened?*
- Now try reversing the order in the last two parts, taking the root first, then the power. What happened?*
- Express these mathematical points using mathematical expressions.*

2. Order of operations

- (a) The order (**PE(MD)(AS)**):
- i. Inside parentheses first (*and absolute value*)
 - ii. Exponents
 - iii. Products and division
 - iv. Addition and subtraction
 - v. Read left to right
- (b) Note: Often put in extra parentheses for emphasis.

PROBLEM 4. *Compute the following*

- i. $7 + 8 \cdot (-1)$
- ii. $(7 + 8) \cdot (-1)$
- iii. $7 \cdot (-3) + 6/2$
- iv. *Consider the last expression.*
 - *Insert parentheses into the last expression so that it is evaluated from left to right. Then evaluate it.*
 - *Insert parentheses into the last expression so that it is evaluated from right to left. Then evaluate it.*
- v. $|-7|$
- vi. $|7|$
- vii. $|-9| - |3 - 8|$
- viii. $3 + (-5)2^3$
- ix. $(-2)^4$ versus -2^4
- x. $(-2)^3$ versus -2^3