## MTH 23 LECTURE NOTES (Ojakian)

# Topic 13: Correlation and Scatter Diagrams

#### **OUTLINE**

References (Algebra Book: None; Statistics Book: 12.2)

- 1. Plotting points
- 2. Correlation

### 1. How are two variables related?

- (a) Example: Guilded Exercise 1 (ch. 4, p. 122, from 5th edition): Look at just table of numbers.
- (b) Two variables are correlated if: The value of one variable can be used to predict the value of the other variable.
- (c) Goal: Determine how correlated two variables are.

**PROBLEM 1.** In the example, guess the work hours lost for various choices of training hours.

## 2. Scatter Diagram

PROBLEM 2. Verify the scatter plot of data for guilded exercise.

- (a) Terminology
  - i. Horizontal axis: Explanatory variable
  - ii. Vertical axis: Response variable
  - iii. Correlation ...
- (b)

**PROBLEM 3.** Make a scatter plot for the following data:

X:4, 7, 8, 12, 17

Y: 2, 5, 10, 11, 20

Does the data look "correlated"? What is its rough shape?

### 3. Correlation Coefficient

- (a) How good is the Best-Fil line?  $\dots$ 
  - Correlation Coefficient = Correl([column 1], [column 2])
- (b) Measures how close to a line the scatter plot looks. Denoted r.
  - i. It is between -1 and 1, inclusive.
  - ii. If r close to 0: Little or no linear correlation.
  - iii. If r close to +1: Positive correlation
  - iv. If r close to -1: Negative correlation

(c)

### PROBLEM 4.

- i. Make up a table of two columns of data, with at least 10 individuals and find the correlation coefficient. Try to choose the data so that r is close to 0.9.
- ii. Make up a table of two columns of data, with at least 10 individuals and find the correlation coefficient. Try to choose the data so that r is close to -0.9.
- iii. Make up a table of two columns of data, with at least 10 individuals and find the correlation coefficient. Try to choose the data so that r is close to 0.

# 4. Applying Correlation

**PROBLEM 5.** Pick two variables from class data that you think might be correlated and check.

### 5. Correlation versus Causation

"Correlation does not imply causation!"

- (a) Lurking variable (or hidden variable): A third variable (not X or Y) that is simultaneously responsible for the changes in X and Y.
- (b)

PROBLEM 6. From section 4.1 (5th edition) do problems: 8, 9.

(c) See webpage: http://www.tylervigen.com/spurious-correlations