

CSI 35 LECTURE NOTES (Ojakian)

Topic 2: Introduction to Mathematical Terminology

OUTLINE

(References: Wells 1 - 4)

1. Mathematical Terminology

1. Terminology about mathematical reasoning

- (a) Theorem, Lemma, Corollary
- (b) Definition (note: some precise definitions omitted in favor of loose description, e.g. the integers)
- (c) Proof

2. Other Terminology

- (a) Integers
- (b) Definition of positive, negative.

PROBLEM 1. *Is 0 positive? Prove your answer.*

- (c) Division ($n|m$)

PROBLEM 2. *How might you define the terminology “even” and “odd”?*

PROBLEM 3. *1) Make up a simple definition, 2) State a theorem that concerns your definition, and 3) Prove your theorem.*

3. Harder Questions?

- (a) Are there infinitely many prime numbers?
- (b) Are there infinitely many twin primes?

4. Programming to test hypothesis

PROBLEM 4. *Write Python programs in SageMath to test the above (use the `Primes()` of SageMath).*