

# CSI 33 LECTURE NOTES (Ojakian)

## Topic 8: Trees

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### OUTLINE

(References: Ch. 6, 7)

1. Trees
  2. Preorder, postorder, inorder
  3. Binary Search Tree
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#### 1. Trees: Basic Terminology

- (a) Vertices, Nodes, Edges
- (b) Rooted vs. non-Rooted Tree
- (c) Root, Parent, Child, Sibling
- (d) Binary Tree
- (e) Example

**PROBLEM 1.** *Discuss a basic decision tree for guessing what animal someone is thinking of (more to come on decision trees later ...).*

#### 2. Programming Binary Trees

- (a)
- (b) Typical “addressing” in binary trees.

**PROBLEM 2.** *Create just a `TreeNode` class and build the above decision tree from scratch.*

**PROBLEM 3.** *Create a `BinaryTree` class that uses this addressing method to: 1) add nodes and 2) get node data.*

#### 3. Application: Data Compression

**PROBLEM 4.** *Consider Problem 8 (pages 249 - 251), and discuss how to do **without** data compression.*

**PROBLEM 5.** *Reconsider the last problem, but now **with** data compression.*

**PROBLEM 6.** *Use the `BinaryTree` class to program the data compression.*

#### 4. Prefix and Postfix Expressions

General Intuition: Reading left to right, for postfix, the operation comes after its two operands, while for prefix, the operation comes before its two operands.

- (a) Recall postfix (philosophy: wait for an operator, then look back at two operands - i.e. operator after operands). We can call this an “Operator Triggered Stack”.
  - i. Read left to right.
  - ii. If next item is an operand, push onto stack.
  - iii. If next item is an operator, pop last two items, evaluate, then push the result on the stack.
  - iv. The single number on the stack at the end is the answer
- (b) Prefix (philosophy: wait for two operands, then look back at the operator - i.e. operator before operands). We can call this an “Operand Triggered Stack”.
  - i. Read left to right.
  - ii. Push the next item onto the stack.
  - iii. If the top two items on the stack are operands, then pop the top two operands and apply the next popped operator, evaluate, then push the result on the stack.
  - iv. The single number on the stack at the end is the answer
- (c) Another approach to Prefix: Do the postfix approach (i.e. Operator Triggered Stack), but from right to left, instead of from left to right.
- (d) Another approach to Postfix: Do the prefix approach (i.e. Operand Triggered Stack), but from left to right, instead of from right to left.

(e)

**PROBLEM 7.** Calculate the following postfix expression:  $5\ 2\ +\ 8\ 3\ -\ *$

(f)

**PROBLEM 8.** Calculate the following prefix expressions

i.  $*\ 9\ +\ 2\ 6$

ii.  $+\ 7\ *\ 45\ +\ 2\ 0$

#### 5. Recursion

- (a) Wrapper function and Recursive Helper function

**PROBLEM 9.** See recursion examples: *Fibonnaci and list sums*

- (b) Check the recursion works using idea of Proof-By-Induction

**PROBLEM 10.** Verify the last recursion examples (*Fibonnaci and list sums*) using *Proof-By-Induction*.

- (c) Recursion on Linked Structures:

- i. Pass a node reference to the recursive function
- ii. Function returns a node reference to the properly modified linked structure
- iii. Notice pattern: link passed-in and the link modified are the same
- iv.

**PROBLEM 11.** Add a recursive *append* and *delete* to linked list, thinking inductively.

Then verify the operation of the functions using *Proof-By-Induction*.

## 6. Expression Tree and Traversals

(a)

**PROBLEM 12.** *For example from book (p. 277, Figure 7.4) do three kinds of traversal.*

(b) Inorder - corresponds infix expression

(c) Postorder - corresponds postfix expression

(d) Preorder - corresponds prefix expression

(e)

**PROBLEM 13.** *Program in-order. Leave other two as group work.*

## 7. Binary Search Tree

(a) Its defining property with examples.

**PROBLEM 14.** *From diagrams, which are and which are not BSTs?*

(b) Recursive and non-recursive insertion: Do examples, code, and prove

(c) Recursive deletion:

i. First just code and discuss the case where the deleted node has **at most ONE child**

ii. Discuss theory for case: deleted node has TWO children

iii. Code must a deleteMax method

iv. Then do full delete method

## 8. Application: Machine Learning and Decision Trees

For all this, see the coding example.

(a) Introduction to Data Frames.

(b) The goal of Machine Learning Classification via the example Data Frame: From features to target.

(c) Majority Vote and Node Purity (understood probabilistically)

(d) How to split node on a feature: Maximize purity (understood probabilistically)