

# MTH 30 LECTURE NOTES (Ojakian)

## Topic 12: Polynomial Division

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### OUTLINE

(References: 3.5, 3.6 (parts) )

1. Polynomial Division
  2. Use in factoring
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#### 1. Recall Long Division with numbers

- (a) Dividend (inside thing dividing into)
- (b) Divisor (what is dividing)
- (c) Quotient (how many times goes in)
- (d) Remainder (leftover)
- (e) Three ways to express result:
  - i. State Quotient and Remainder
  - ii. Express just Dividend (i.e. =  $(Quotient)(Divisor)+Remainder$ ), the “division algorithm”
  - iii. Express rational expression Dividend/Divisor

#### 2. Division with Algebraic Expressions

Do the above with algebra.

- (a) Problems from Section 3.5: 14, 15, 17, 21, 39, 41, 49

#### 3. Remainder Theorem

**Theorem 1.** *If a polynomial  $p(x)$  is divided by  $(x - k)$ , then the remainder is  $p(k)$*

#### 4. Rational Zeroes Theorem

- (a) Applies to a polynomial with integer coefficients.
- (b) Limits the CANDIDATE rational zeroes to those of the form  $\frac{p}{q}$ , where  $p$  divides the constant term and  $q$  divides the leading coefficient.