MTH 28.5 LECTURE NOTES (Ojakian) Topic 29: Radical Arithmetic

OUTLINE

References: 8.4, 8.5

1. <u>Rules</u>

- (a) Radicals i. $\sqrt[n]{A \cdot B} = \sqrt[n]{A} \cdot \sqrt[n]{B}$ ii. $\sqrt[n]{\frac{A}{B}} = \frac{\sqrt[n]{A}}{\sqrt[n]{B}}$ iii. $\sqrt[n]{A^n} = A \text{ (for } A \ge 0)$ (b) Exponents i. $A^n \cdot A^m = A^{n+m}$ ii. $\frac{A^n}{A^m} = A^{n-m}$
 - iii. $(A \cdot B)^n = A^n B^n$ iv. $\left(\frac{A}{B}\right)^n = \frac{A^n}{B^n}$ v. For $A \ge 0$: $(A^n)^m = A^{nm}$

2. Simplification Requirements

(a) No exponents are negative.

Example: x^3y^{-4} should be simplified to $\frac{x^3}{u^4}$

- (b) Nothing can be pulled out of a radical. Example: $\sqrt[3]{16}$ should be simplified to $2\sqrt[3]{2}$.
- (c) All the exponent rules (from the key rules above) should be carried out. Example: x^3x^5 simplifies to x^8 .
- (d) Exponents on numbers should be evaluated, left as a simplified radical if need be. Example: 25^{1/2} should be simplified to 5. Example: 8^{1/2} should be simplified to 2√2.
- (e) There are no radical symbols in the denominator.

Example: $\frac{1}{\sqrt{5}}$ should be simplified to $\frac{\sqrt{5}}{5}$

3. Division - Radical Expressions

PROBLEM 1. Simplify the following:

(a)
$$\frac{3}{\sqrt{6}}$$

(b) $\sqrt{\frac{18m^5n^6}{p^{12}q^4}}$
(c) $\sqrt{\frac{4}{49AC^2}}$
(d) $\frac{10mn}{\sqrt{5mn}}$

4. Add/Subtract - Radical Expressions

PROBLEM 2. Simplify the following.

(a)
$$\sqrt{2} + 3\sqrt{2}$$

(b) $\sqrt[3]{4} - 5\sqrt[3]{4}$
(c) $\sqrt{75} + \sqrt{48} - 7\sqrt{12}$
(d) $\sqrt{20} + \sqrt[3]{54} - 2\sqrt{45} + \sqrt{7} + 10\sqrt[3]{16} - 4\sqrt[3]{3000}$
(e) $3\sqrt{8}(2\sqrt{10} - \sqrt{27})$
(f) $(\sqrt{5})^2 + (\sqrt{3})^2$
(g) $(\sqrt{5} + \sqrt{3})^2$