MTH 28.5 LECTURE NOTES (Ojakian)

Topic 4: Exponents and Order of Operations

OUTLINE References (1.5)

- 1. Exponents
 - (a) Evaluating expression with exponents
 - (b) Expressing a product using exponents
- 2. Order of operations
- 1. Evaluating expression with exponents

PROBLEM 1. Evaluate the following

- (a) 2^3
- $(b) 3^2$
- $(c) 118^1$
- $(d) (-2)^3$
- $(e) \ (-2)^4$
- $(f) (-1)^{557}$
- $(g) \ (-1)^{502}$
- $(h) \,\, 0^{53}$

PROBLEM 2. Using the examples from the previous problem describe a rule for answering this question: When a negative number is raised to an exponent, is it positive or negative?

2. Exponents: Negative sign done first or second?

Issue: $(-2)^4$ versus -2^4

- (a) The first means: (-2)(-2)(-2)(-2), which is 16
- (b) The second means: (-1) · 2⁴, which = (-1)(16) = −16
 PROBLEM 3. Compute the following
 - *i.* $(-4)^2$ *ii.* -4^2 *iii.* $(-4)^3$ *iv.* -4^3

3. Express product in exponential form

PROBLEM 4. Write each product using exponents; do not evaluate.

(a) $4 \cdot 4 \cdot 4 \cdot 4 \cdot 4 \cdot 4$ (b) $(-9) \cdot (-9) \cdot (-9) \cdot (-9) \cdot (-9)$

4. When Order Does Not Matter

PROBLEM 5. Notice the changing of orders in the following computations. Figure out when the order matters and when it does not.

 $\begin{array}{l} (a) \ 5-2 \\ (b) \ 2-5 \\ (c) \ 5+2+(-4) \\ (d) \ 2+(-4)+5 \\ (e) \ (2)(-4)(3) \\ (f) \ (-4)(3)(2) \\ (g) \ 6\div2 \end{array}$

 $(h) \ 2 \div 6$

Recall the following facts.

Theorem. (Addition Fact) A sum can be evaluated in any order.

Theorem. (Product Fact) A product can be evaluated in any order.

5. Order of operations

(a) The order (PE(MD)(AS)):

- i. Inside parentheses first (and absolute value)
- ii. Exponents
- iii. Products and division
- iv. Addition and subtraction
- v. Read left to right
- (b) Note: Often put in extra parentheses for emphasis.

PROBLEM 6. Compute the following

- *i.* $7 + 8 \cdot (-1)$
- *ii.* $(7+8) \cdot (-1)$
- *iii.* $7 \cdot (-3) + 5 \cdot 2$
- iv. Insert parentheses into the last expression so that it is evaluated from left to right. Then evaluate it.
- v. Insert parentheses into the last expression so that it is evaluated from right to left. Then evaluate it.

PROBLEM 7.

i. $4 + 8 \div 2 - (7)(-3)$ ii. |-7| - |3 - 7|iii. $3 + (-1)2^4$ iv. $3 + (-2)^4$ v. $- - -(-2)^3$ vi. $-(--2)^3 - (-1)^{177}$

6. Distributive Property

PROBLEM 8. Compute

(a) 2(-3+4)(b) (2)(-3) + (2)(4)(c) (6+3)(-2)(d) (6)(-2) + (3)(-2)

PROBLEM 9. Based on problem 8, complete the following theorem.

Theorem. (Distributive Property) For any real numbers a, b, c the following are true:

- $a \cdot (b+c) = \dots$ [Fill It IN]
- $(b+c) \cdot a = \dots$ [Fill It IN]

7. Group Work: Order of Operations Game