CSI 35 LECTURE NOTES (Ojakian)

Topic 6: Relations

OUTLINE

(References: Wells 51 - 53, 55 - 59, 117, 129, 130, 132 - 137; Rosen: 9.1, 9.2, 9.3)

- 1. Relations: Definitions and Examples
- 2. Database Application
- 3. Properties: Functional, Reflexivie, Symmetric, Antisymmetric, Transitive

1. Relations

- (a) Binary and n-ary
 - i. Subset of Cartesian product.
 - ii. Notations: $(a, b) \in R$, or R(a, b), or aRb.
 - iii. Do some small finite examples.
- (b) Some more involved examples.
 - i. < on the rationals
 - ii. Congruence $\bmod n$
 - iii. (x, x^2) and (x^2, x) , for x real.
 - iv. $\{(x, y, z, n) \mid x, y, z, n \text{ are positive integers and } x^n + y^n = z^n\}$

2. Representing Relations (mostly binary ones)

- (a) Table or listing
- (b) Graph "on the plane"
- (c) Two columns with arrows
- (d) Digraph
- (e) Matrix

3. Functions

- (a) Example: (x, x^2) versus (x^2, x) from above.
- (b) Definition of "functional relation" or a "relation which is a function".
- (c) The "Vertical Line Test".
- (d) Consider some small finite examples, some are, some are not.

4. Viewed as databases

Do in theory and sqlite.

- (a) Examples 11 and 12 (Section 9.2)
- (b) Have various "tables"
 - i. Each column has a name and type
 - ii. Each row is an item
 - iii. Entire table can be viewed as n-ary relation
- (c) Create table
 - i. "CREATE TABLE [table] ([col1] [type1], [col2] [type2], ...)"
- (d) Build database with Insert command
 - i. "INSERT INTO [table] VALUES (value1 , value2, value3 ...)"
- (e) Retreive data with Select command
 - i. "SELECT [columns] FROM [table] WHERE columns = [...]"

5. Typical Properties for Binary Relations on a Set

- (a) Definition: Binary relation on a set.
- (b) Reflexive
 - i. Example: \leq and <
- (c) Symmetric (and anti-Symmetric)
 - i. Example: Congruence and \leq
 - ii. Do Rosen 9.1, 49 (Mistaken Proof).
- (d) Transitive
 - i. Example: \leq
 - ii. Hasse Diagrams for Transitive relations

6. Examples for Reflexive, Symmetric, and Transitive

PROBLEM 1. Do Wells 59.1.3

PROBLEM 2. Do Wells 55.1.9.

PROBLEM 3. Do Wells 56.1.4.

PROBLEM 4. Do Wells 59.1.4.

PROBLEM 5. Begin Wells 58.1.10 (finishing it will be a question on the next class work).

7. More Exercises

- (a) Section 9.1: 2, 3, 4, 6, 7, 10
- (b) Section 9.2: 2, 28b
- (c) Section 9.3 (skip any "irreflexive"): 1 10, 22 32