

CSI 30 LECTURE NOTES (Ojakian)

Topic 14: Probability

OUTLINE

(References: 7.1)

1. Probability

1. Opening Question

Monty Hall Problem.

2. Basic Terminology

- (a) Example: Roll die, and different possibilities.
- (b) Sample space. Along with assumption: equally likely outcomes.
- (c) $P(E) = \frac{\text{Event Size}}{\text{Sample Space Size}}$
- (d) See above examples with this formula
- (e) Note: $0 \leq P(E) \leq 1$

3. More Examples

- (a) Urns with different balls. Taking one ball.
- (b) Two dice questions (sum being a value)

4. Complements

- (a) Example: NOT rolling something?
- (b) $P(\overline{E}) = 1 - P(E)$

5. Inclusion-Exclusion (for probability)

- (a) Simple Example:
 - i. 7 students from The Bronx (3 of which are math majors), 3 from Manhattan (1 is a math major). Question: Prob(From the Bronx or a math major).
 - ii. Note: If you just add, you get a probability above 1!
- (b) $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
- (c) Example 9.

6. Exercises

- (a) Section 7.1: 1 - 6, 22, 23