## BRONX COMMUNITY COLLEGE of the City University of New York

## DEPARTMENT OF MATHEMATICS & COMPUTER SCIENCE

 $\begin{array}{l} \text{MATH 23 (JP)} \\ \text{Fall 2017} \end{array}$ 

THIRD EXAM Due Date: 11/15/2017

- 1. (5 points) Explain with your own words what we understand by a random variable. What is the difference between discrete and continuous random variables?
- 2. The following probability distribution represents the claim sizes (x) for an auto insurance policy.

x	1	2	3	4
P(x)	.1	.2	.25	

- (a) (5 points) Complete the be to be a discrete probability distribution.
- (b) (5 points) Sketch the bar graph of the distribution.
- (c) (5 points) Calculate the expected value of the distribution.
- (d) (5 points) Calculate the standard deviation.
- 3. (5 points) Explain what we understand by Binomial experiment. Give an example of a variable following a binomial distribution.
- 4. Suppose that the probability of a hurricane in a calendar year is p = .05. Find the probability that, in a 10-year period, we have:
  - (a) (5 points) Exactly 1 hurricane.
  - (b) (5 points) At least 3 hurricanes.
  - (c) (5 points) At most 2 hurricanes.
- 5. (10 points) Assuming that the probability of having a daughter is of the 50%.
  - (a) (5 points) What is the probability of having exactly 1 daughter in a family with 5 kids?
  - (b) (5 points) What is the expected value of the number of daughters in families with 5 kids?
  - (c) (5 points) What is the standard deviation ?
- 6. Sketch a graph that represents the following probabilities, when Z is distributed standard normal and find the actual probabilities
  - (a) (5 points) P(z < 1.75)
  - (b) (5 points) P(z > 1.83)
  - (c) (5 points) P(-0.41 < z < 1.32)
- 7. (5 points) Explain with your words what we understand by a sampling distribution.
- 8. The average salary for first-year teacher is 28,340. If the distribution is approximately normal with  $\sigma = 3250$ , what is the probability that a randomly selected first-year teacher makes these salaries?
  - (a) (5 points) More than 30,000 a year
  - (b) (5 points) Between 20,000 and 35,000 a year.

- (c) (5 points) Suppose that random samples of 10 teachers are selected to obtain a statistic  $\bar{X}$ . What can you say about the  $\bar{X}$ -distribution? What would be the approximated values of the mean  $\mu_{\bar{X}}$  and the standard deviation  $\sigma_{\bar{X}}$ ?
- (d) (5 points) Suppose that 10 teachers are selected at random, what is the probability that the mean salary  $\bar{x}$  is more than 30,000?