## BRONX COMMUNITY COLLEGE of the City University of New York

## DEPARTMENT OF MATHEMATICS \& COMPUTER SCIENCE

1. (5 points) Explain with your own words what we understand by a random variable. What is the difference between discrete and continuous random variables?
2. The following probability distribution represents the claim sizes $(x)$ for an auto insurance policy.

| x | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{x})$ | .1 | .2 | .25 |  |

(a) (5 points) Complete the be to be a discrete probability distribution.
(b) (5 points) Sketch the bar graph of the distribution.
(c) (5 points) Calculate the expected value of the distribution.
(d) (5 points) Calculate the standard deviation.
3. (5 points) Explain what we understand by Binomial experiment. Give an example of a variable following a binomial distribution.
4. Suppose that the probability of a hurricane in a calendar year is $p=.05$. Find the probability that, in a 10 -year period, we have:
(a) (5 points) Exactly 1 hurricane.
(b) (5 points) At least 3 hurricanes.
(c) (5 points) At most 2 hurricanes.
5. (10 points) Assuming that the probability of having a daughter is of the $50 \%$.
(a) (5 points) What is the probability of having exactly 1 daughter in a family with 5 kids?
(b) (5 points) What is the expected value of the number of daughters in families with 5 kids?
(c) (5 points) What is the standard deviation?
6. Sketch a graph that represents the following probabilities, when $Z$ is distributed standard normal and find the actual probabilities
(a) (5 points) $P(z<1.75)$
(b) (5 points) $P(z>1.83)$
(c) (5 points) $P(-0.41<z<1.32)$
7. (5 points) Explain with your words what we understand by a sampling distribution.
8. The average salary for first-year teacher is 28,340 . If the distribution is approximately normal with $\sigma=3250$, what is the probability that a randomly selected first-year teacher makes these salaries?
(a) (5 points) More than 30, 000 a year
(b) (5 points) Between 20, 000 and 35,000 a year.
(c) (5 points) Suppose that random samples of 10 teachers are selected to obtain a statistic $\bar{X}$. What can you say about the $\bar{X}$-distribution? What would be the approximated values of the mean $\mu_{\bar{X}}$ and the standard deviation $\sigma_{\bar{X}}$ ?
(d) (5 points) Suppose that 10 teachers are selected at random, what is the probability that the mean salary $\bar{x}$ is more than 30,000 ?

