## BRONX COMMUNITY COLLEGE of the City University of New York

## DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE

MATH 06 Fall 2014

Third Exam Day (2 Hours)

1. (12 points) Simplify the following expressions:

(a) 
$$2\sqrt[3]{24} - 4\sqrt[3]{81} + 3\sqrt[3]{3}$$

(b) 
$$(3 - \sqrt{2})^2$$

(c) 
$$32^{3/5}$$

(d) 
$$(8x^6y^10)^{-1/3}$$

(e) 
$$(-3+5i)(1+2i)$$

(f) 
$$\frac{1+3i}{2-3i}$$

2. (24 points) Simplify:

(a) 
$$\frac{x^2-1}{x^2+2x+1} \div \frac{x-1}{2x^2-x-3}$$
 (a')  $\frac{3x+7}{x+5} + \frac{2x+18}{x+5}$  (b)  $\frac{a-b}{5} - \frac{31-4b}{4}$  (b')  $\frac{3x}{x+5} - \frac{5x}{x-3}$  (c)  $\frac{3x-7}{x^2-4} + \frac{2x-18}{x^2-3x+2}$  (c')  $\frac{4x^2-25}{x^2+x-12} \cdot \frac{2x^2-6x}{4x^2-10x}$  (d)  $\frac{3}{x-4} - 2$  (d')  $\frac{1}{x-1} + 1$ 

$$(a')$$
  $\frac{3x+7}{x+5} + \frac{2x+18}{x+5}$ 

(b) 
$$\frac{a-b}{5} - \frac{31-4b}{4}$$

$$(b') \quad \frac{3x}{x+5} - \frac{5x}{x-3}$$

(c) 
$$\frac{3x-7}{x^2-4} + \frac{2x-18}{x^2-3x+2}$$

$$(c')$$
  $\frac{4x^2-25}{x^2+x-12} \cdot \frac{2x^2-6x}{4x^2-10x}$ 

(d) 
$$\frac{\frac{3}{x-4}-2}{1-\frac{4}{x-4}}$$

$$(d')$$
  $\frac{\frac{1}{x-1}+1}{\frac{1}{x-1}-1}$ 

3. (12 points) Given the quadratic function  $f(x) = 3x^2 - 6x - 9$ .

- (a) Find the y-intercept.
- (b) Find the x-intercepts.
- (c) Find the vertex.
- (d) Sketch the graph.
- 4. (5 points) Solve the equation  $\frac{5}{3x-2} = \frac{3}{2x+4}$ .
- 5. (5 points) Solve the equation  $3^{2x-1} = 1/81$ .
- 6. (10 points) Given the functions  $f(x) = 2^x$  and  $g(x) = \log_2(x)$ :

| (x) |
|-----|
|     |
|     |
|     |
|     |
|     |
|     |
|     |
|     |

(a) Complete the table

(b) Sketch the graph of f and g in the same axis of coordinates.

- 7. (8 points) Compute the x in each case by changing to exponential form:
  - a)  $\log_2(x) = 5$ ,
- $b)\log_x(3) = 2$
- $c) \log_8(4) = x$   $d) \log_{27}(1/9) = x$

- 8. (5 points) If an anle  $\theta$  in the third quadrant has  $\sin(\theta) = -3/5$ . Find the value of  $\cos(\theta)$  and  $\tan(\theta)$ .
- 9. (10 points) Complete the table with the exact value of each trigonometric function:

| Angle     | sin | $\cos$ | tan | cot | sec | csc |
|-----------|-----|--------|-----|-----|-----|-----|
| 135°      |     |        |     |     |     |     |
| 750°      |     |        |     |     |     |     |
| $-4\pi/3$ |     |        |     |     |     |     |
| $9\pi/4$  |     |        |     |     |     |     |
| 420°      |     |        |     |     |     |     |
| 240°      |     |        |     |     |     |     |

- 10. (5 points) Verify the identity:  $\csc(\theta) \tan(\theta) \cos(\theta) = 1$ .
- 11. (8 points) Sketch one cycle of the graph of  $f(x) = -3\sin(4x)$ . Identify Amplitude (A), Period (T) and Phase Shift. Identify Zeroes, Maxima and Minima.