## BRONX COMMUNITY COLLEGE

## DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE

MATH 06
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Exam 1
March 10, 2011

Name: $\qquad$

Directions: Write your answers in the provided booklets. Make sure to indicate which answer belongs to which question. To get full credit you must show all your work. Simplify your answers whenever possible. Be certain to indicate your final answer clearly. Each problem is worth 5 points

1. Sketch a graph of the parabola $y=-x^{2}-2 x+3$. The graph should correctly indicate the vertex, the axis of symmetry, the $x$-intercepts, the $y$-intercept and the point symmetric to the $y$-intercept.

2. Evaluate (give exact answer). Simplify your answer as much as possible.

$$
\sin 30^{\circ} \cos 45^{\circ}+\sin 45^{\circ} \cos 30^{\circ}
$$

3. Simplify: $\quad 3 \sqrt{20}-2 \sqrt{45}+4 \sqrt{125}$
4. Simplify: $(\sqrt{3}+\sqrt{2})(\sqrt{3}-\sqrt{2})$
5. Simplify: $(3-2 \sqrt{5})^{2}$
A. $8^{-\frac{2}{3}}$
B. $\sqrt[3]{27 x^{7} y^{8} z^{9}}$
C. $\frac{6}{\sqrt{3}}$
6. Rationalize the denominator. Simplify your answer as much as possible.

$$
\frac{2 \sqrt{10}}{3-\sqrt{5}}
$$

8. Simplify. If needed assume that all variables represent positive numbers.

$$
2 \sqrt[4]{x^{3}}\left(\sqrt[4]{16 x}-3 \sqrt[4]{x^{5}}+\sqrt[4]{x^{3}}\right)
$$

9. Simplify assuming all variables represent positive numbers. The answer should contain only positive integers as exponents.

$$
\left(\frac{x^{-6} y^{5}}{z^{\frac{2}{3}}}\right)^{\frac{3}{2}}
$$

10. Simplify, assuming all variables represent positive numbers: $\sqrt{\frac{12 x^{9} y^{4}}{25 z^{5}}}$
11. Solve $\sqrt{x+19}+x=1$.
12. Solve $\sqrt{x+6}=1+\sqrt{x+1}$
13. Solve $x^{2}-4=2 x$
14. Solve $6 x^{2}-x-1=0$
15. One leg of a right triangle is 5 inches and the hypotenuse is 10 inches. Find the length of the other leg.
16. Find the area of the following triangle, if $\theta=63.43^{\circ}$.

17. Find the coordinates of the point $P$, if its distance from the origin is 2.8 units and the angle that $O P$ forms with the $x$-axis is $65^{\circ}$, as shown in the figure below.

18. Find the angle $\theta$ :

19. The angle of elevation to the top of a building, measured from a point 100 feet away from the base of the building is $60^{\circ}$. Find the height of the building. Give exact answer.
20. A boat is observed from the top of a lighthouse, 300 feet above sea level. If the boat is 3000 feet away what's the angle of depression?
