## Eighth Set of Homework for Math 05

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Please note: You should fully justify your answers.

## 1 Slope

1. Find the slope of the following pair of points:
(a) $P(2,3), Q(4,5)$
(b) $M(-2,-2), N(3,-5)$
(c) $P(0,-3), Q(3,5)$
(d) $M(-2,4), N(8,-6)$
(e) $S(0,5), P(3,0)$
(f) $P(-1,-4), Q(-3,-10)$
(g) $O(0,0), P(-1,4)$
(h) $S(2,-3), T(-4,-3)$
(i) $P(-1,4), Q(1,-4)$
(j) $A(2,-5), Q(2,1)$
(k) $A\left(\frac{2}{3}, 1\right), B=\left(\frac{5}{3},-\frac{1}{2}\right)$
2. For each set of points decide if they are collinear, that is whether they lie on the same line.
(a) $A(2,4), B(-3,-6), C(5,10)$
(b) $P(2,4), Q(4,10), R(-1,5)$
(c) $O(0,0), M(-2,-8), N(5,15)$
(d) $M(2,2), N(3,3), L(-5,-5)$
(e) $P(3,4), Q(-2,4), R(-5,3)$
(f) $A(1,2), B(3,4), C(5,7)$
(g) $M(-2,-3), N(1,-3), L(7,-3)$
(h) $P(11,4), Q(11,-7), R(11,8)$
3. For each of the following equations find the slope of the line they represent by finding two points in the line and using the formula.
(a) $y=3 x-2$
(b) $-2 x+4 y=-6$
(c) $x=-5 y-7$
(d) $3 x-2 y=6$
(e) $3(y-2)=-5(2 x-1)+3$
4. Find the slope for each of the lines in Figure 1.
5. Put each of the following equations into slope-intercept form. What is the slope and what is the $y$ intercept of the line each equation represents?
(a) $x=-2 y-6$


Figure 1: The lines of Question 4
(b) $-10 x-5 y=7$
(c) $-4 x+2 y-10=0$
(d) $3 x-15 y-5=0$
(e) $3 y=-8$
(f) $-7 x+28 y-15=0$
(g) $-2(5 x-5)=3(4 y-2)+8$
6. A linear equation is in general form if it is written as:

$$
\begin{equation*}
A x+B y+C=0 \tag{1}
\end{equation*}
$$

where $A, B, C$ are real numbers and at least one of the $A, B$ is not zero. Find a formula for the slope and the $y$-intercept of the line with equation (1), when they exist.
7. Use the formulas you found in Question 6 to find the slope and the $y$-intercept of each of the following lines:
(a) $2 x+y-6=0$
(b) $3 x+5 y-10=0$
(c) $4 x-2 y+7=0$

