

BRONX COMMUNITY COLLEGE
of the City University of New York

DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE

MATH 05
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Exam 1
September 13, 2016

Directions: Write your answers in the provided space. To get full credit you *must* show all your work. Simplify your answers whenever possible. Be certain to indicate your final answer clearly. This exam contains 100 points.

1. Which of the following is *larger*?

(a) (2 points) $\frac{5}{12}$ $\frac{7}{12}$

A. The first. **B. The second.** C. They are equal.

(b) (2 points) $\frac{5}{12} = \frac{15}{36}$ $\frac{4}{9} = \frac{16}{36}$

A. The first. **B. The second.** C. They are equal.

(c) (2 points) $\frac{5}{12} = \frac{15}{36}$ $\frac{5}{9} = \frac{20}{36}$

A. The first. **B. The second.** C. They are equal.

(d) (2 points) $\frac{5}{7} = \frac{10}{14}$ $\frac{10}{14}$

A. The first. B. The second. **C. They are equal.**

(e) (2 points) $-\frac{5}{12}$ $-\frac{7}{12}$

A. The first. B. The second. C. They are equal.

(f) (2 points) $\left| -\frac{2}{3} \right| = \frac{2}{3} = \frac{4}{6}$ $\left| -\frac{1}{2} \right| = \frac{1}{2} = \frac{3}{6}$

A. The first. B. The second. C. They are equal.

2. Perform the following operations. Simplify your answers as much as possible:

(a) (2 points) $\frac{1}{8} + \frac{3}{8} = \frac{4}{8} = \frac{1}{2}$

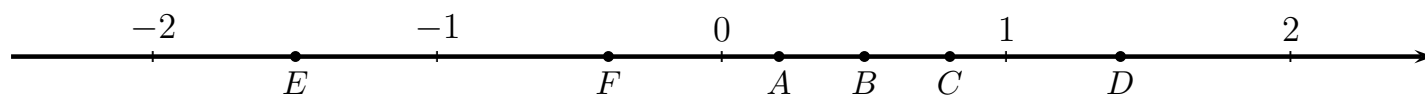
(b) (2 points) $\frac{5}{9} - \frac{8}{9} = -\frac{3}{9} = -\frac{1}{3}$

(c) (2 points) $\frac{5}{6} - \frac{2}{3} = \frac{5}{6} - \frac{4}{6} = \frac{1}{6}$

(d) (2 points) $\frac{3}{5} + \frac{7}{4} = \frac{12}{20} + \frac{35}{20} = \frac{47}{20}$

(e) (2 points) $\left(-\frac{3}{5}\right) + \frac{7}{4} = \left(-\frac{12}{20}\right) + \frac{35}{20} = \frac{23}{20}$

3. Indicate which point in the number line below corresponds to which number.



(a) (2 points) Point F corresponds to $-\frac{2}{5}$

(b) (2 points) Point B corresponds to $\frac{1}{2}$

(c) (2 points) Point A corresponds to $\frac{1}{5}$

(d) (2 points) Point C corresponds to $\frac{4}{5}$

(e) (2 points) Point D corresponds to $\frac{7}{5}$

(f) (2 points) Point E corresponds to $-\frac{3}{2}$

4. (4 points) Evaluate: $(a - b)^2$, when $a = -1$, and $b = 2$. $\left((-1) - (2)\right)^2 = (-3)^2 = 9$
 A. 5 B. -5 **C. 9** D. 1

5. (4 points) Evaluate: $-x^2 + 2x$, when $x = 3$. $-(3)^2 + 2(3) = -9 + 6 = -3$
A. -3 B. 3 C. -15 D. 15

6. (5 points) Evaluate: $5 - 3(4 - 3) - 2^3 \div 8 \cdot 4 = 5 - 3(1) - 2^3 - 8 \cdot 4$
 $= 5 - 3(1) - 8 - 8 \cdot 4$
 $= 5 - 3 - 1 \cdot 4$
 $= 5 - 3 - 4$
 $= 2 - 4$
 $= -2$

7. (5 points) Evaluate: $\frac{-16}{9} \cdot \frac{18}{-25} \cdot \left(-\frac{10}{6}\right) \cdot \frac{-5}{4} \cdot \frac{3}{4} = 2$

8. (5 points) Evaluate: $\frac{-2^2 + 3(6 - 4)}{12 - (3 - 7)^2} = \frac{-2^2 + 3(2)}{12 - (-4)^2}$
 $= \frac{-4 + 3(2)}{12 - (16)}$
 $= \frac{-4 + 6}{-4}$
 $= \frac{2}{-4}$
 $= -\frac{1}{2}$

9. (5 points) Evaluate: $\frac{2 - \frac{3}{2}}{\frac{1}{2} + \frac{3}{4}} = \frac{\frac{4}{2} - \frac{3}{2}}{\frac{2}{4} + \frac{3}{4}} = \frac{\frac{1}{2}}{\frac{5}{4}} = \frac{1}{2} \cdot \frac{4}{5} = \frac{2}{5}$

10. (5 points) Evaluate the expression $\sqrt{b^2 - 4ac}$, when $a = -2$, $b = -3$, and $c = 2$.

$$\begin{aligned}\sqrt{(-3)^2 - 4(-2)(2)} &= \sqrt{9 - 4(-2)(2)} \\ &= \sqrt{9 - (-8)(2)} \\ &= \sqrt{9 + 16} \\ &= \sqrt{25} \\ &= 5\end{aligned}$$

11. (5 points) Evaluate the expression $\frac{y_2 - y_1}{x_2 - x_1}$, when $x_1 = 1$, $x_2 = -3$, $y_1 = -3$, and $y_2 = -9$.

$$\begin{aligned}\frac{(-9) - (-3)}{(-3) - (1)} &= \frac{(-9) + 3}{(-3) + (-1)} \\ &= \frac{-6}{-4} \\ &= \frac{3}{2}\end{aligned}$$

12. (5 points) Evaluate the expression $x^2 - 2xy + y^2$, when $x = 3$ and $y = -2$.

$$\begin{aligned}(3)^2 - 2(3)(-2) + (-2)^2 &= 9 - 2(3)(-2) + 4 \\ &= 9 - (6)(-2) + 4 \\ &= 9 - (-12) + 4 \\ &= 9 + 12 + 4 \\ &= 25\end{aligned}$$

13. (5 points) Evaluate $a^2 - b^2$, when $a = 3$ and $b = -3$. $(3)^2 - (-3)^2 = 9 - 9 = 0$

A. 18 B. -18 **C. 0** D. 12

14. (5 points) Evaluate the expression $\frac{-x^2 + 3}{2 - x}$ when $x = -2$.

$$\frac{-(-2)^2 + 3}{2 - (-2)} = \frac{-4 + 3}{2 + 2} = \frac{-1}{4} = -\frac{1}{4}$$

A. $\frac{1}{4}$ **B. $-\frac{1}{4}$** C. $\frac{12}{5}$ D. -12

15. (3 points) If $x = -\frac{3}{2}$ then $4x^2 + 4x - 3 = 0$

A. True B. False.

$$\begin{aligned}4\left(-\frac{3}{2}\right)^2 + 4\left(-\frac{3}{2}\right) - 3 &= 0 \\ \cancel{4}\left(\frac{9}{\cancel{4}}\right) + \cancel{4}\left(-\frac{3}{\cancel{2}}\right) - 3 &= 0\end{aligned}$$

$$9 + (-6) - 3 = 0$$

$$3 - 3 = 0$$

16. (3 points) If x represents an unknown number then 8 subtracted from three times that number is represented by the expression:

- A. $3x - 8$ B. $8 - 3x$ C. $3(x - 8)$ D. $3(8 - x)$

17. (3 points) If y represents an unknown number then 8 divided by twice that number is represented by the expression:

- A. $8 - 2y$ B. $2y - 8$ C. $\frac{2y}{8}$ D. $\frac{8}{2y}$

18. (4 points) Write a mathematical expression that represents the following phrase:

The sum of four times a number and six, divided by nine more than the same number.

$$\frac{4x+6}{x+9}$$