

EXERCISES.

- (1) Verify that the following are pairs of inverse functions:
- $f(x) = 3x - \frac{1}{2}$, $g(x) = \frac{2y + 1}{6}$
 - $f(x) = \sqrt[3]{x + 5}$, $g(x) = x^3 - 5$
 - $g(x) = \frac{3x - 2}{2x + 3}$, $h(x) = -\frac{3x + 2}{2y - 3}$
 - $h(x) = x^2 - 3$ with domain $[0, \infty)$, $g(x) = \sqrt{x + 3}$
 - $f(x) = 2 - \sqrt{x + 7}$, $h(x) = x^2 - 4x - 3$ with domain $(-\infty, 2]$
 - $f(x) = \log_{10}(3x - 5)$, $g(x) = \frac{10^x + 5}{3}$
- (2) Are the functions $f(x) = x^2$ and $g(x) = \sqrt{x}$ inverses?
- (3) A function is called an *involution* if it is its own inverse. In other words, a function f is an involution if for all x in the domain of f , we have that $(f \circ f)(x) = x$. Show that the following functions are involutions:
- $f(x) = \frac{1}{x}$
 - $g(x) = \sqrt{16 - x^2}$ with domain $[0, 4]$
 - $f(x) = \frac{2x - 3}{4x - 2}$
- (4) Extra Credit Is the function $f(x) = \sqrt{16 - x^2}$ with domain $[-4, 0]$ an involution? Justify your answer.
- (5) Extra Credit Is it possible to restrict the domain of the function $f(x) = 4x$ so that it becomes an involution?
- (6) For the following pair of functions determine the compositions $f \circ g$ and $g \circ f$. In each case you should give the domain as well as the formula.
- $f(x) = 3x - 1$, $g(x) = 2x + 3$
 - $f(x) = x - 2$, $g(x) = 5x^2 - 2$
 - $f(x) = x^2 - 3x + 5$, $g(x) = 2x - 3$
 - $f(x) = -2x^2 + x - 4$, $g(x) = x^2 + 1$
 - $f(x) = x^2 - 4$, $g(x) = \sqrt{x + 3}$
 - $f(x) = \frac{2x - 1}{5x + 3}$, $g(x) = \frac{x + 2}{x + 1}$
 - $f(x) = \sqrt{x - 3}$, $g(x) = 3 - x$
 - $f(x) = \frac{2x}{x^2 - 4}$, $g(x) = \frac{1}{x} - 2$
 - $f(x) = x^2 + 4$, $g(x) = \sqrt{3 - x}$
 - $f(x) = x$, $g(x) = 2^{\sin x}$
 - $f(x) = -x$, $g(x) = \sqrt{x}$
 - $f(x) = 3$, $g(x) = x^2 - 5x + 5$
 - $f(x) = x^2 + 3x - 7$, $g(x) = \sqrt{x - 1} + 1$
 - $f(x) = \cos 3x$, $g(x) = x^2 - 1$
 - $f(x) = \log_2 x$, $g(x) = -\sqrt{x + 3}$
- (7) If $f(0) = -4$ and $g(-4) = 6$ what is $(g \circ f)(0)$?
- (8) The graph of the functions f and g are shown in Figure 1. Find the following values:
- $(f \circ g)(0)$
 - $(f \circ g)(-2)$
 - $(g \circ f)(1)$
 - $(g \circ f)(-1)$
 - $(g \circ f)(-4)$

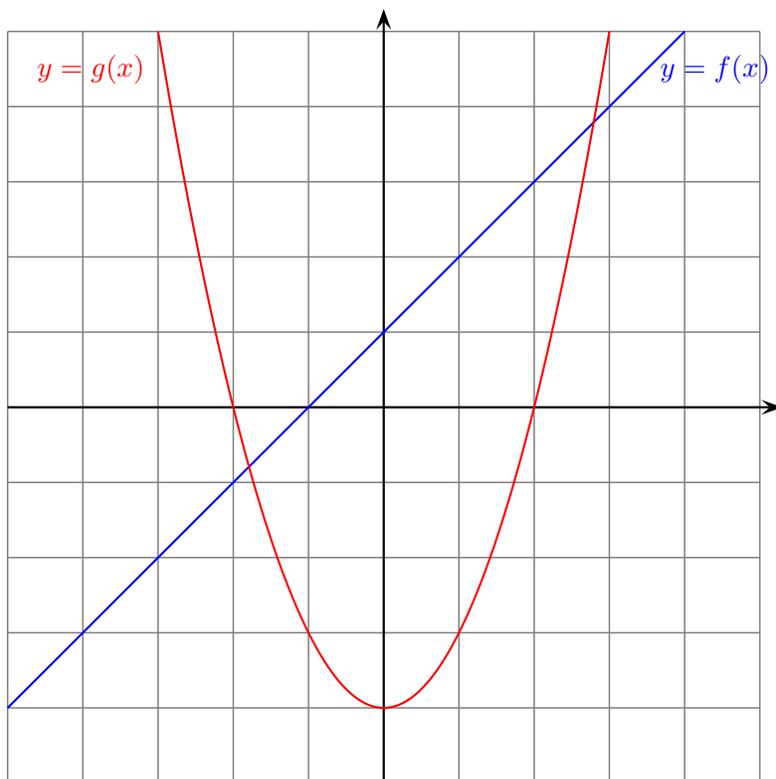


FIGURE 1. Two functions

- (9) Let $l(x) = x + 3$. For each of the following functions f ,
- find $f \circ l, l \circ f$
 - graph $y = f(x), y = (f \circ l)(x), (l \circ f)(x)$ on the same grid.
- (a) $f(x) = x^2$
 (b) $f(x) = -x^2$
 (c) $f(x) = x^3$
 (d) $f(x) = |x|$
- (10) Repeat the previous exercise with $l(x) = x - 2$