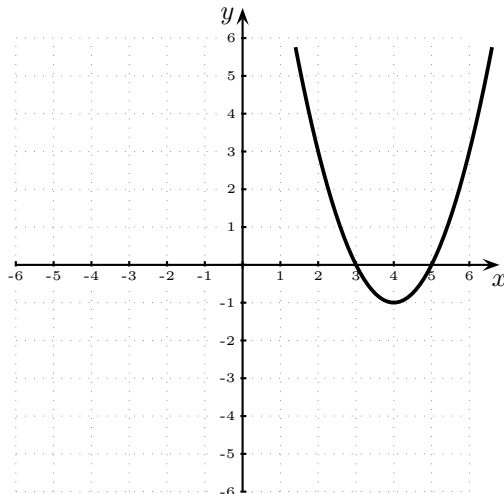


SOLUTION

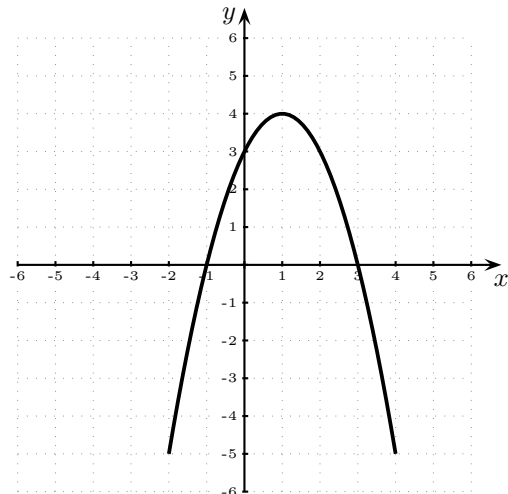
1. For the following quadratic functions,
 - Find the vertex and x - and y -intercepts.
 - Give the equation of the axes of symmetry.
 - Draw the graph in the axes provided,
 - Determine the function's domain and range.

a) $f(x) = (x - 4)^2 - 1$.



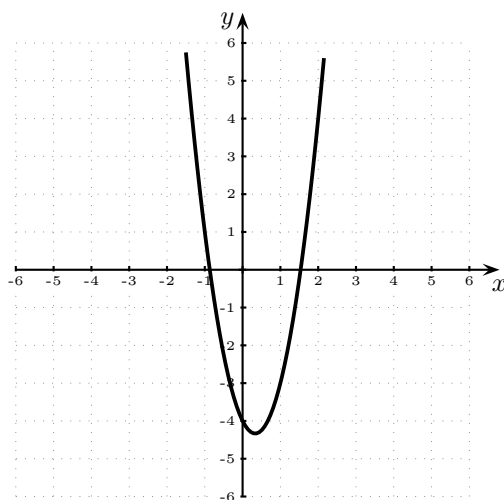
Vertex: $(4, -1)$
 y -intercept: 5. **x -intercepts:** 3, 5
Axes of symmetry: $x = 4$
Domain: \mathbb{R} . **Range:** $[-1, \infty)$

b) $g(x) = 4 - (x - 1)^2$.



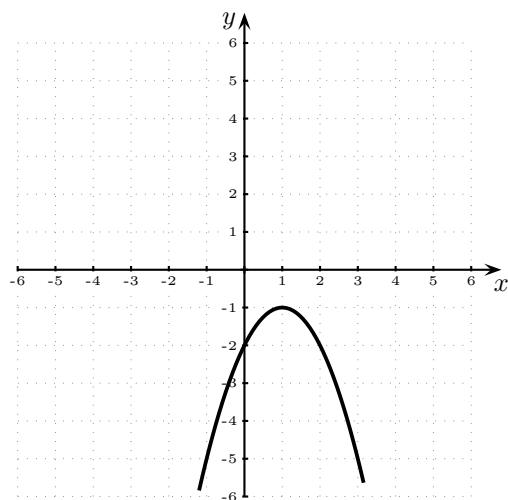
Vertex: $(1, 4)$
 y -intercept: 3. **x -intercepts:** $-1, 3$
Axes of symmetry: $x = 1$
Domain: \mathbb{R} . **Range:** $(-\infty, 4]$

c) $h(x) = 3x^2 - 2x - 4$.



Vertex: $(1/3, -13/3)$
 y -intercept: -4 . **x -intercepts:** $\frac{1 \pm \sqrt{13}}{3}$
Axes of symmetry: $x = 1/3$
Domain: \mathbb{R} . **Range:** $[-13/3, \infty)$

d) $i(x) = 2x - x^2 - 2$.



Vertex: $(1, -1)$
 y -intercept: -2 . **x -intercepts:** NONE
Axes of symmetry: $x = 1$
Domain: \mathbb{R} . **Range:** $(-\infty, 1]$

2. For each of the following functions, find

- (i) The end behaviour of the graph.
- (ii) The y -intercept.
- (iii) For exercises **a**), **b**), **c**), the x -intercepts with their multiplicity and the local behaviour at the x -intercepts.
- (iv) Do the graphs of all the functions using any graphing device. For example, use <https://www.desmos.com/calculator>
Check that the end behaviour of the graphs that you found in part (i) are all correct.

a) $f(x) = 2(x - 2)^2(x + 1)$

b) $f(x) = -2x^2(x - 2)(x + 2)^2$

c) $f(x) = 3x(x + 1)^2(x - 1)^3$

d) $f(x) = -x^4 + 5x^2 + x$

Solution:

(i) End behavior: **a)** ↙ ↗ **b)** ↖ ↘ **c)** ↖ ↗ **d)** ↙ ↘

(ii) y intercept: **a)** $y = 8$. **b)** $y = 0$. **c)** $y = 0$. **d)** $y = 0$.

(iii) x intercepts:

a) $x = 2$, multiplicity 2, ∩ or ∪; $x = -1$, multiplicity 1, ∩ or ∪.

b) $x = 0$, multiplicity 2, ∩ or ∪; $x = 2$; mult. 1, ∩ or ∪; $x = -2$; mult. 2, ∩ or ∪.

c) $x = 0$, multiplicity 1, ∩ or ∪; $x = -1$, multiplicity 2, ∩ or ∪; $x = 1$, mult. 3, ∩ or ∪.

Do the graphs with your favorite graphing device to see the solution.