MTH~28,~Midterm~2,~V.~4,~10/29/25~ Prof. Luis Fernández

NAME:

There are 19 questions. Some are multiple choice and some are free response.

Each question is worth 6 points over 100 (so 14 points are extra credit).

For multiple-choice questions, just circle your answer.

For free-response questions, SHOW ALL WORK to receive credit.

1. Add and simplify.

$$\frac{x-1}{x+4} + \frac{x+3}{x+2}$$

2. Simplify the rational expression.

$$\frac{x^2 - 2x - 8}{x - 4}$$

3. Simplify the expression $\frac{x^2 - 4}{x^2 - 3x + 2}$

$$\frac{x^2 - 4}{x^2 - 3x + 2}$$

4. Multiply and simplify your answer.

$$\frac{x-4}{x} \cdot \frac{x^2+3x}{x^2-x-12}$$

5. Multiply and simplify
$$\frac{x^2 - x - 30}{x^2 - 10x + 24} \cdot \frac{x^2 - 16}{x^2 + 8x + 16}$$

6. Divide and simplify your answer.

$$\frac{x^2+7x}{10} \div \frac{x+7}{2}$$

7. Divide and simplify your answer.

$$\frac{x^2 - 25}{x^2 - 11x + 30} \div \frac{x}{x - 6}$$

8. Multiply and simplify your answer.

$$\frac{x^2-4}{x^2-3x+2} \cdot \frac{x-1}{x}$$

9. Add and simplify

$$\frac{5}{x^2} + \frac{2}{x^2 + x}$$

10. Add and simplify

$$\frac{5}{y-3} + \frac{3}{y+5}$$

11. Match the expressions below with the letters labeling their equivalent expressions.

$$2. \frac{1}{x+3} + \frac{1}{x^2+9}$$

A.
$$\frac{x+4}{x^2-9}$$

B.
$$\frac{x^2 + x + 6}{(x - 3)(x^2 + 9)}$$

C.
$$\frac{x^2 + x + 12}{(x+3)(x^2+9)}$$

12. Subtract and simplify

$$\frac{1}{x+3} - \frac{1}{x+4}$$

13. Simplify the expression

$$\frac{1 + \frac{4}{c - 4}}{1 - \frac{4}{c - 4}}$$

14. Simplify the expresion

$$\frac{\frac{x^3}{x-7}}{\frac{x^7}{x^7}}$$

15. Subtract and simplify
$$\frac{2x}{x^2 + 3x - 4} - \frac{1}{x - 1}$$

16. Solve the following equation:

$$x + \frac{1}{x} = 2$$

17. Solve the equation: $\frac{x}{4x-12} - \frac{x-4}{x-3} = 1$.

18. Solve the following equation:

$$\frac{x+1}{x-1} = \frac{-10}{x+3} + \frac{8}{x^2 + 2x - 3}$$

19. Solve the following equation:

$$\frac{4}{x^2 - 25} + \frac{3}{x - 5} = \frac{2}{x + 5}$$