

NAME: _____ SOLUTION _____

There are 25 questions. Some are multiple choice and some are free response. Each question is worth 4 points over 100, except question 2 which is worth 12 points (so 8 points are extra credit). For multiple-choice questions, just circle your answer. For free-response questions, SHOW ALL WORK to receive credit.

1. Write the expression $\sqrt[3]{-72}$ in simplest radical form.

Solution: $\boxed{-2\sqrt[3]{9}}$

2. Simplify each of the following:

Solution:

(a) $\sqrt{32} = \boxed{4\sqrt{2}}$

(b) $\sqrt{27} = \boxed{3\sqrt{3}}$

(c) $\sqrt{18} = \boxed{3\sqrt{2}}$

(d) $\sqrt{50} = \boxed{5\sqrt{2}}$

(e) $\sqrt{72} = \boxed{6\sqrt{2}}$

(f) $\sqrt{300} = \boxed{10\sqrt{3}}$

3. Evaluate the expression: $125^{-\frac{2}{3}}$

Solution: $\boxed{\frac{1}{25}}$

4. Write the expression

$$\left(\frac{x^3y}{y^2}\right)^{6/7}$$

in the form $\frac{x^r}{y^t}$.

Solution: $\boxed{\frac{x^{\frac{18}{7}}}{y^{\frac{6}{7}}}}$

5. Write the expression

$$\left(\frac{a^{-3}}{3b^{-1/6}}\right)^{-1}$$

in the form $\frac{n \cdot a^r}{b^t}$.

Solution: $\boxed{\frac{3a^3}{b^{\frac{1}{6}}}}$

6. Write using rational exponents: $\sqrt[3]{x^{10}}$

Solution: $\boxed{x^{\frac{10}{3}}}$

7. Write the expression

$$\sqrt{108} - \sqrt{48}$$

in the form $A\sqrt{C}$.

Solution: $\boxed{2\sqrt{3}}$

8. Find the product

$$(-5\sqrt{3})(4\sqrt{5})$$

and write it in simplest radical form $A\sqrt{C}$.

Solution: $\boxed{-20\sqrt{15}}$

9. Multiply and simplify

$$(8 + 2\sqrt{2})(8 - 2\sqrt{2})$$

Circle the answer.

Solution:

(a) 72

(b) $72 + 32\sqrt{2}$

(c) $72 - 32\sqrt{2}$

(d) 56

10. Simplify.

$$-4\sqrt{27} - 2\sqrt{12} - 2\sqrt{147}$$

Circle the answer.

Solution:

(a) $-30\sqrt{3}$

(b) $-30\sqrt{9}$

(c) $-8\sqrt{3}$

(d) $-8\sqrt{27}$

11. Multiply and simplify

$$(3 + 2\sqrt{7})^2$$

Circle the answer.

Solution:

(a) $37 - 12\sqrt{7}$

(b) 35

(c) $37 + 12\sqrt{7}$

(d) $23 + 12\sqrt{7}$

12. Simplify completely

$$\frac{\sqrt{2}\sqrt{30}}{\sqrt{5}}$$

Circle the answer.

Solution:

(a) $3\sqrt{2}$

(b) $2\sqrt{3}$

(c) $4\sqrt{3}$

(d) $\sqrt{12}$

13. Subtract and simplify

$$7\sqrt{8} - 9\sqrt{18}$$

Solution:

14. Simplify the expression

$$\sqrt{\frac{75}{11}},$$

and write it in the form $\frac{A\sqrt{B}}{C}$.

Solution: $\boxed{\frac{5\sqrt{33}}{11}}$.

15. Rationalize (that is, write without radicals in the denominator):

$$\frac{\sqrt{13} - \sqrt{3}}{\sqrt{13} + \sqrt{3}}$$

Solution: $\boxed{\frac{8 - \sqrt{39}}{5}}$

16. Solve the equation

$$\sqrt{2x - 1} - 5 = 0$$

Solution: $\boxed{x = 13}$

17. Solve the equation

$$\sqrt{2x + 1} = 3\sqrt{x - 1}$$

Solution: $\boxed{x = \frac{10}{7}}$

18. Solve the equation

$$\sqrt{4x} = x - 3.$$

Solution: $x = 9$

(Note that there is another “solution”, $x = 1$, but it does not work.)

19. Write $\sqrt{-32}$

as the product of a real number and i .

Circle the answer.

Solution:

(a) $2\sqrt{4}i$

(b) $4\sqrt{2}i$

(c) $-2\sqrt{4}i$

(d) $-4\sqrt{2}$

20. Evaluate the expression

$$(7 + 2i) + (-5 + 7i)$$

and write the result in the form $a + bi$.

Solution: $2 + 9i$

21. Evaluate the expression

$$(-1 + 3i) - (7 - 3i)$$

and write the result in the form $a + bi$.

Solution: $-8 + 6i$

22. Multiply

$$(-11 - 6i)(-8 - 9i)$$

Solution: $\boxed{34 + 147i}$.

23. Evaluate the expression

$$\frac{-3 + i}{1 + 4i}$$

and write the result in the form $a + bi$.

Solution: $\boxed{\frac{1 - 13i}{-3}}$.

24. Solve the quadratic equation

$$3x^2 + 8x - 3 = 0$$

and write the solutions in simplified form.

Solution: $\boxed{x = -3 \text{ and } x = \frac{1}{3}}$.

25. Solve the quadratic equation

$$x^2 - 5x - 5 = 0$$

and write the solutions in simplified form.

Solution: $\boxed{x = \frac{5 + 3\sqrt{5}}{2} \text{ and } x = \frac{5 - 3\sqrt{5}}{2}}$.