MTH 05, Test 2, V. 1b, 10/23/18 Luis Fernández

NAME: SOLUTION

There are twenty-two questions, each worth 5 points. For multiple-choice questions, circle your answer. For free-response questions, SHOW ALL WORK to receive credit.

- 1. Solve for t in the expression A = rt 3.
- (a) t = 3
- (b) t = Ar + 3
- (c) $t = \frac{A+3}{r}$ (d) $t = \frac{r}{A} + 3$

2. Solve for t in the equation $P = \frac{t}{4} + a$. (a) $t = \frac{P-a}{4}$

(b)
$$t = 4a + P$$

(c) $t = \frac{P - 4a}{2}$
(d) $t = 4(P - a)$

- **3.** The area A of a trapezoid is given by the formula $A = \frac{B+b}{2} \cdot h$. If A = 90, B = 6, and b = 3, what is the value of h?
- (a) 18
- ((b)) 20
- (c) $\frac{99}{2}$
- (d) -53

4. What is the slope-intercept form of the equation 5x - 4y = 20?

(a)
$$y = \frac{4}{5}x + 4$$

(b) $y = 5x + 24$
(c) $y = \frac{3}{2}x + 3$
(d) $y = \frac{5}{4}x - 5$

- 5. Use the formula $F = \frac{9}{5}C + 32$ to find F when C = 15.
- ((a)) 59
- (b) -4
- (c) 37
- (d) 81.2

6. What is the slope of the line connecting the points (4, 10) and (6, 3)?

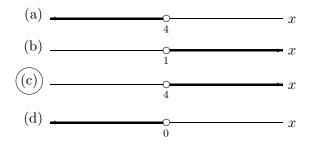
(a)
$$-\frac{7}{2}$$

(b) $\frac{13}{10}$
(c) 4
(d) $\frac{1}{4}$

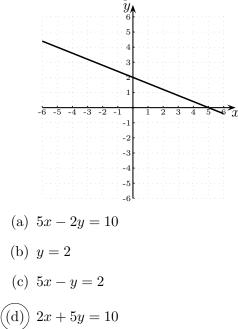
- 7. Find x-intercept and y-intercept for the graph of the equation 2x 7y = 14.
- (a) x-intercept: (-14, 2) and y-intercept: (7, 14)
- (b) x-intercept: (-7, 0) and y-intercept: (0, 2)
- ((c)) x-intercept: (7,0) and y-intercept: (0,-2)
- (d) x-intercept: (0,0) and y-intercept: (2,7)

- 8. Find the slope and y-intercept for the graph of the equation 3x + 7y = 28.
- (a) Slope = $-\frac{3}{7}$ and *y*-intercept: (0,4)
- (b) Slope $=\frac{3}{7}$ and *y*-intercept: (0, -4)
- (c) Slope $=\frac{3}{7}$ and *y*-intercept: (4,0)
- (d) Slope $= -\frac{3}{7}$ and *y*-intercept: (0, 28)

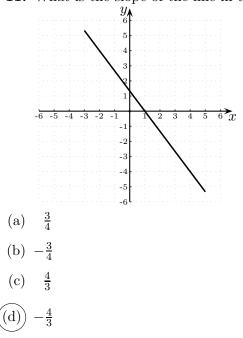
9. Pick the graph of the solution to the inequality 10x - 10 > 6x + 6.



10. Choose the equation of the line in the graph.



11. What is the slope of the line in the graph?



- 12. Find the equation of the horizontal line passing through the point (-3, -4).
- (a) y = -4(b) x = -3(c) $y = \frac{3}{4}x$ (d) $y = \frac{4}{3}x$

13. Which equation's graph is parallel to that of y = 3x - 14?

14. Solve:
$$\frac{3x}{7} \le \frac{15}{14}$$
(a) $x \ge \frac{5}{2}$
(b) $x < \frac{2}{5}$
(c) $x \le \frac{5}{2}$
(d) $x = 5$

Free response questions start here. SHOW ALL WORK!!!

15. Find the slope and y-intercept of the line with equation 2x + 5y = 15.

Solution:

(a)) y = 3x + 12

(b) y = -3x + 8

(c) $y = \frac{1}{3}x + 7$

(d) $y = -\frac{1}{3}x - 11$

Let us write the equation in slope-intercept form. To this end, solve for y: If 2x + 5y = 15then, subtracting 2x from both sides we get 5y = -2x + 15, and then dividing both sides by 5 we get

$$y = -\frac{2}{5}x + 3.$$

Therefore the slope is $-\frac{2}{5}$ and the *y*-intercept is 3.

16. Solve and graph the solution on the number line: $3-5(2x+5) \ge 2(x+4)-7x$.

Solution:

Expand and combine like terms first: $3-5(2x+5) \ge 2(x+4) - 7x$ $3-10x-25 \ge 2x+8-7x$ $-10x-22 \ge -5x+8$ Subtract 8 from both sides: $-10x-30 \ge -5x$ Add 10x to both sides: $-30 \ge 5x$ Divide by 5: $-6 \ge x \text{ (or } x \le -6).$

$$\bullet$$
 -6 x

17. Find an equation for the line passing through the points (2,5) and (-2,7).

Solution:

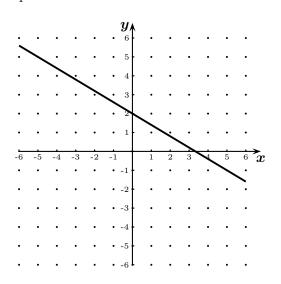
The slope of the line is:

$$m = \frac{7-5}{-2-2} = \frac{2}{-4} = -\frac{1}{2}.$$

Since it passes through the point (2, 5), we can use the point-slope form to obtain the equation sought:

$$y - 5 = -\frac{1}{2}(x - 2).$$

19. Graph $y = -\frac{3}{5}x + 2$ indicating at least two points.



Solution: Two points: (0, 2), (5, -1)

18. Find the equation of the line passing through the point (5, -2) and perpendicular to the line -2x + 5y = 1.

Solution:

The slope of the given line is found by solving for y and finding the number that multiplies x:

$$-2x + 5y = 1 \rightarrow 5y = 2x + 1 \rightarrow y = \frac{2}{5}x + \frac{1}{5}.$$

Therefore the slope of the given line is $\frac{2}{5}$.

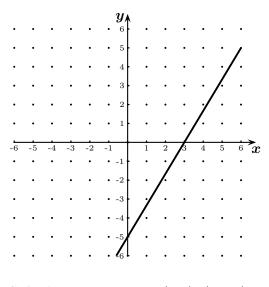
Since the line whose equation we want to find is perpendicular to the given one, its slope has to be the opposite reciprocal of the slope we found above. That is, the slope of the line whose equation we want is

$$m = -\frac{5}{2}.$$

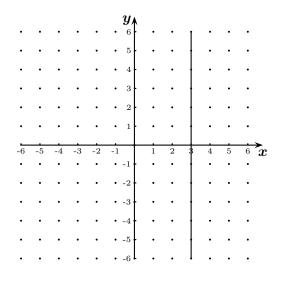
Since it passes through (5, -2), we can use the point-slope form to obtain the equation sought:

$$y - (-2) = -\frac{5}{2}(x - 5).$$

20. Graph 5x - 3y = 15 indicating at least two points.



Solution: Two points: (3, 0), (0, -5)



Solution: Two points: (3,0), (3,1)

22. Solve the following system of equations. If there is no unique solution, say whether the system has *no solutions* or *infinitely many solutions*.

$$\begin{cases} 3x + 2y = 10\\ 5x - 3y = 4 \end{cases}$$

Solution:
First multiply the first equation by (-5) and
the second by 3 to get
$$\begin{cases} -15x - 10y = -50\\ 15x - 9y = 12 \end{cases}$$

Add the equations to get $-19y = -38$, which
gives $y = 2$.
Now multiply the first equation by 3 and the
second by 2 to get
$$\begin{cases} 9x + 6y = 30\\ 10x - 6y = 8 \end{cases}$$

Add the equations to get $19x = 38$. Divide
both sides by 2 to obtain $x = 3$.
Therefore the solution is (2, 2).

21. Graph the equation x = 3 indicating at least two points.