# BRONX COMMUNITY COLLEGE <br> of the City University of New York 

DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE

MTH 30
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Exam 2 REVIEW
Fall 2023

## Directions: REVIEW FOR TEST 2

1. Consider the function $f$ given in the table below. No work required on this problem.

| $x$ | 2 | -4 | 6 | -10 | 0 | -17 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 0 | -6 | -10 | -2 | 6 | 1 |

Use the table to evaluate the following:
a. $f(0)$
b. $f(-10)$
c. $f^{-1}(0)$
d. $f^{-1}(1)$
e. $f^{-1}(-2)$
2. Consider the graph of the equation $y=x^{2}+9 x+20$. Find all its intercepts ( x and y intercepts).
3. Consider the graph of the equation $y=x^{2}+x-20$. Find all its intercepts ( x and y intercepts).
4. Suppose $f(x)=-5 x+2$. Find the inverse $f^{-1}(x)$ using algebra.
5. For each pair of functions determine if they are inverses of eachother by checking if $f(g(x))=x$ and $g(f(x))=x$.
a. Check if the following two function are inverses: $f(x)=x+4$ and $g(x)=x-4$
b. Check if the following two function are inverses: $f(x)=x+3$ and $g(x)=x+3$
c. Check if the following two function are inverses: $f(x)=7 x$ and $g(x)=(1 / 7) x$
6. Consider the linear functions, $f(x)=2 x+2$ and $g(x)=2 x-3$ and $h(x)=-4 x+1$.

For each pair determine if they intersect or not. If they intersect, find the intersection point.
7. Solve each of the following equations (note that they use absolute values).
a. Solve $|x|=405$
b. Solve $|y-10|=405$
c. Solve $|y+10|=405$
d. Solve $|5 y+10|=405$
e. Solve $5|y+10|=405$
f. Solve $5|5 y+10|=405$
8. Solve each of the following inequalities (note that they use absolute values).
a. Solve $|x|<10$
b. Solve $|x| \geq 10$
c. Solve $|-2 x|<10$
d. Solve $-2|x|<10$
e. Solve $-2|-2 x|>10$
f. Solve $-2|-2 x|-2<10$
g. Solve $-2|-2 x|-2 \geq 10$
9. For each of the two functions do this: a) Graph it, b) Find its domain and range, c) Is the function one-to-one, d) Does the function have an inverse, e) If the function has an inverse, find the domain and range of its inverse.
a. $g(x)=4 x^{8}$
b. $h(x)=4 x^{3}$
c. $f(x)=2+\frac{1}{x-3}$
10. Let $f(x)=(-4 / 3) x-1$. Find the slope and all intercepts. Then graph the function.
11. Graph $f(x)=x^{3}$. Then do the following:
a. Let $g(x)=(x+2)^{3}+2$

Describe how the graph of $g$ is a transformation of the graph of the original function $f$. Then graph $g$.
b. Let $h(x)=4-x^{3}$

Describe how the graph of $h$ is a transformation of the graph of the original function $f$. Then graph $h$.
12. Consider the graph of the function $f(x)=-x^{2}-3 x+1$.
a. Does $f(x)$ open up or open down?
b. Find the equation of its axis of symmetry.
c. Find the vertex.
d. What is the maximum and minimum value of $f(x)$ ? (if it does not have one of these, then state that)
e. Draw a rough graph of $f(x)$ (i.e., do not worry about intercepts, but label the vertex and get shape roughly correct).

