## BRONX COMMUNITY COLLEGE of the City University of New York

## DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE

MTH 30 Kerry Ojakian Exam 2 REVIEW Fall 2023

## **Directions:** REVIEW FOR TEST 2

1. Consider the function f given in the table below. No work required on this problem.

x	2	-4	6	-10	0	-17
f(x)	0	-6	-10	-2	6	1

Use the table to evaluate the following:

- a. f(0)
- b. f(-10)
- c.  $f^{-1}(0)$
- d.  $f^{-1}(1)$
- e.  $f^{-1}(-2)$
- 2. Consider the graph of the equation  $y = x^2 + 9x + 20$ . Find all its intercepts (x and y intercepts).
- 3. Consider the graph of the equation  $y = x^2 + x 20$ . Find all its intercepts (x and y intercepts).
- 4. Suppose f(x) = -5x + 2. Find the inverse  $f^{-1}(x)$  using algebra.
- 5. For each pair of functions determine if they are inverses of eachother by checking if f(g(x)) = x and g(f(x)) = x.
  - a. Check if the following two function are inverses: f(x) = x + 4 and g(x) = x 4
  - b. Check if the following two function are inverses: f(x) = x + 3 and g(x) = x + 3
  - c. Check if the following two function are inverses: f(x) = 7x and g(x) = (1/7)x

- 6. Consider the linear functions, f(x) = 2x + 2 and g(x) = 2x 3 and h(x) = -4x + 1. For each pair determine if they intersect or not. If they intersect, find the intersection point.
- 7. Solve each of the following equations (note that they use absolute values).
  - a. Solve |x| = 405
  - b. Solve |y 10| = 405
  - c. Solve |y + 10| = 405
  - d. Solve |5y + 10| = 405
  - e. Solve 5|y+10| = 405
  - f. Solve 5|5y + 10| = 405
- 8. Solve each of the following inequalities (note that they use absolute values).
  - a. Solve |x| < 10
  - b. Solve  $|x| \ge 10$
  - c. Solve |-2x| < 10
  - d. Solve -2|x| < 10
  - e. Solve -2|-2x| > 10
  - f. Solve -2|-2x|-2 < 10
  - g. Solve  $-2|-2x|-2 \ge 10$
- 9. For each of the two functions do this: a) Graph it, b) Find its domain and range, c) Is the function one-to-one, d) Does the function have an inverse, e) If the function has an inverse, find the domain and range of its inverse.
  - a.  $g(x) = 4x^8$ b.  $h(x) = 4x^3$ c.  $f(x) = 2 + \frac{1}{x-3}$

10. Let f(x) = (-4/3)x - 1. Find the slope and all intercepts. Then graph the function.

- 11. Graph  $f(x) = x^3$ . Then do the following:
  - a. Let  $g(x) = (x+2)^3 + 2$ Describe how the graph of g is a transformation of the graph of the original function f. Then graph g.
  - b. Let  $h(x) = 4 x^3$ Describe how the graph of h is a transformation of the graph of the original function f. Then graph h.

- 12. Consider the graph of the function  $f(x) = -x^2 3x + 1$ .
  - a. Does f(x) open up or open down?
  - b. Find the equation of its axis of symmetry.
  - c. Find the vertex.
  - d. What is the maximum and minimum value of f(x)? (if it does not have one of these, then state that)
  - e. Draw a rough graph of f(x) (i.e., do not worry about intercepts, but label the vertex and get shape roughly correct).