Please use lots of space and explain your answers, showing clearly any work you had to do. Each question is worth 3 points for a total of 21.
(1) Let $A$ be the $4 \times 2$ matrix $\left[a_{i j}\right]=\left[\begin{array}{cc}2 & 5 \\ 3 & 4 \\ 1 & 0 \\ 8 & -9\end{array}\right]$
(a) What is $a_{11}$ ?
(b) What is $a_{32}$ ?
(c) Write the fourth row as a $1 \times 2$ matrix.
(d) Give $A^{t}$, the transpose of $A$. (Hint: Your answer should be a $2 \times 4$ matrix.)
(2) For the matrices $M=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$ and $N=\left[\begin{array}{cc}2 & 3 \\ -1 & 0\end{array}\right]$ calculate
(a) $M+N$
(b) $M N$
(c) $N^{2}$
(Hint: for parts (b) and (c) you should be using matrix multiplication, meaning rows of the first matrix times columns of second. Also $N^{2}$ just means $N N$.)
(3) Let $M=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$ again.
(a) Write down the identity matrix $I_{2}$.
(b) Compute: $I_{2} M$
(c) Compute: $\mathrm{MI}_{2}$
(4) For the zero-one matrices $A=\left[\begin{array}{ll}0 & 1 \\ 0 & 1\end{array}\right]$ and $B=\left[\begin{array}{ll}1 & 0 \\ 1 & 1\end{array}\right]$ calculate
(a) $A \wedge B$
(b) $A \vee B$
(c) $A \odot B$
(5) Show all the steps used by the procedure max we saw in class to find the biggest number in the list: $3,4,8,2$
(6) Give an algorithm to find the sum of all the integers in a list. First describe your algorithm in words, then write it in pseudocode. It should look like a simpler version of the procedure max.
(7) Show all the steps used by the procedure binary search we saw in class to search for 8 in the ordered list: $2,4,7,8,9$. Make a table showing the values of $i, j$ and $m$ at each step. So the first row in the table has $i=1, j=5$ and $m$ is computed to be 3 . What is the output?

If you get stuck on a question or aren't sure if you understand it:

- Go over the relevant class notes and section in the textbook.
- Check if you get the right answer for a similar odd-numbered question in the textbook (answers at the back of the book).
- Ask me about it after class.
- Come to my office hours: Tue 3-4, Wed 3-4 in CP 317.
- Go to the Math Tutorial Lab in-person in CP 303 or online.

